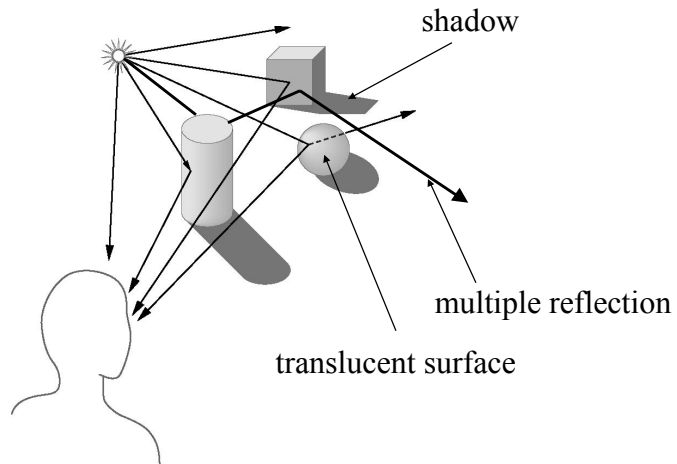


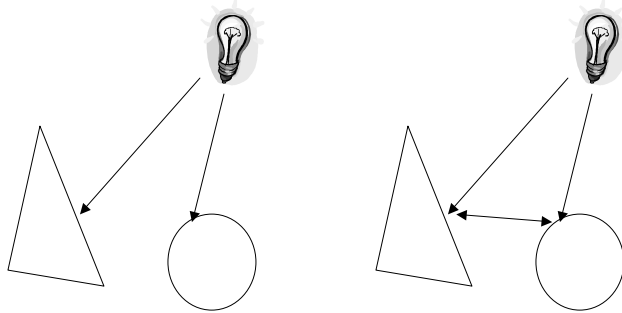
Global Illumination

CS5500 Computer Graphics
May 29, 2006

Global Effects



Local vs. Global



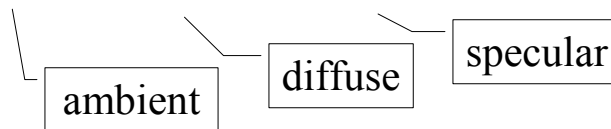
Local vs Global Rendering

- Correct shading requires a global calculation involving all objects and light sources
 - Incompatible with pipeline model which shades each polygon independently (local rendering)
- However, in computer graphics, especially real time graphics, we are happy if things “look right”
 - Exist many techniques for approximating global effects

Local Reflection Models

Phong Reflection Model

- $I = K_a * I_a + k_d * I_d + K_s * I_s$



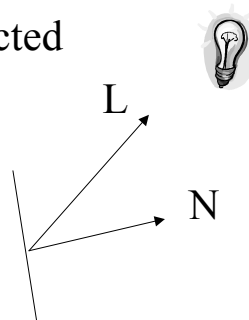
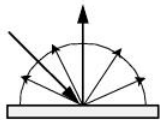
- Not completely correct, but good enough.

Ambient Component

- Accounting for light scatter around.
- I_a is constant.

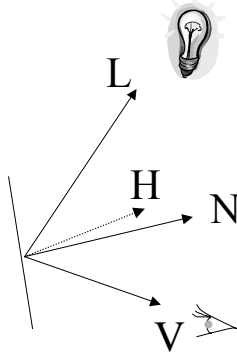
Diffuse Component

- $I_a = I_i * N \cdot L$
- Not affected by viewing direction.
 - i.e., incoming light is reflected to all directions.



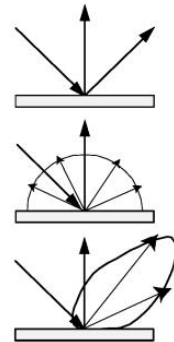
Specular Component (Phong Reflection Model)

- To model imperfect reflection.
- $I_s = I_i(N \cdot H)^n$



Specular Component (Cook & Torrance Model)

- Consider specular reflection as perfect reflection of micro-facets.
- $\text{Specular} = DGF / (N \cdot V)$
 - D: Distribution term
 - G: Geometry (shadowing and masking) term
 - F: Fresnel term

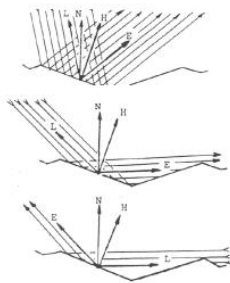


D Term (Cook & Torrance)

- Modeling the distribution of micro-geometry.
- Gaussian distribution can be used:

$$D = k e^{-(\alpha/m)^2}$$

G Term (Cook & Torrance)



$$G = \min(G_a, G_b, G_c)$$

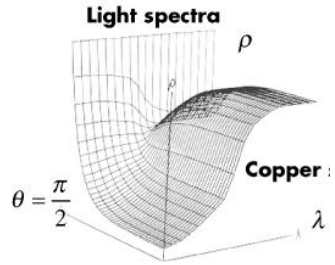
$$G_a = 1$$

$$G_b = \frac{2(\mathbf{N} \cdot \mathbf{H})(\mathbf{N} \cdot \mathbf{E})}{(\mathbf{H} \cdot \mathbf{E})}$$

$$G_c = \frac{2(\mathbf{N} \cdot \mathbf{H})(\mathbf{N} \cdot \mathbf{L})}{(\mathbf{H} \cdot \mathbf{L})}$$

The Fresnel Term

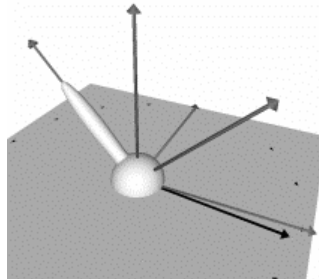
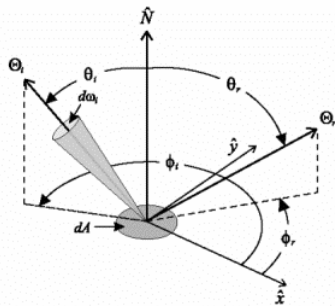
- Color of reflected light varies with viewing angle.



Reflectance of Copper as a function of wavelength and angle of incidence

BRDF

- $BRDF = f(\theta_{in}, \phi_{in}, \theta_{ref}, \phi_{ref}) = f(\text{Light}, \text{View})$



Why Not Always Using BRDF?

- Difficult to find a “closed form” representation of BRDF.
- The Phong model and Cook & Torrance model are approximation of BRDF.
 - They are not 100% matche of BRDF, but they are easy to compute.

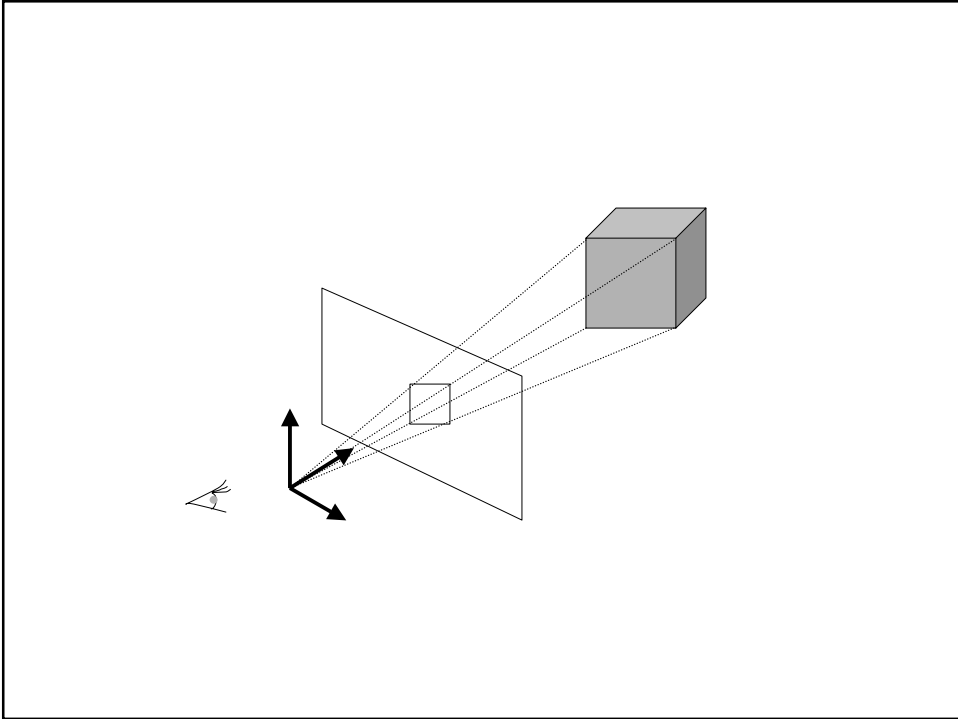
Exercise

- Q1: Those reflectance models give us local illumination only. Why?
Hint: What are the parameters? Do they include the other objects?
- Q2: What typical effects are missing?
Shadow, reflection, and refraction...

Object-Order vs. Screen-Order Rendering

How Do You Draw a Picture (Without a Computer)?

- What is your subject?
- Viewing Parameters:
 - Camera, Picture Frames, Resolutions
- Many ways to specify it:
 - (1) eye, focus length, image plane
 - (2) eye, direction, FOV, up vector



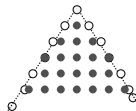
Method A: Object Order Algorithm
(Process one polygon at a time.)

3D to 2D Projection

- OK, so we can map a 3D point (or vertex) to 2D image.
- But what about a 3D surface?
- Polygons are made from points.
- Actually, we only need triangles!

Scan Conversion

- Also called rasterization.
- The 3D to 2D Projection gives us 2D vertices (points).
- We need to fill in the interior.



Shading

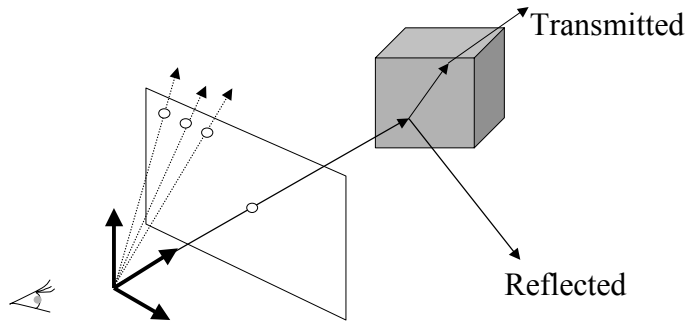
- Interpolation between any two vertices:
 - Vertex colors (lit or unlit?)
 - Normal vectors
 - Z
 - w (or $1/w$) for perspective correction
 - Texture coordinates

Note that we usually apply only local illumination in object order algorithm (because you have to go beyond the current object to obtain the global effect.)

Method B: Screen Order Algorithm
(Process one pixel at a time.)

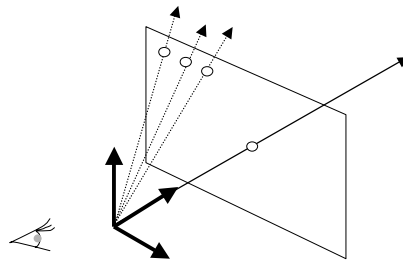
Ray Tracing Algorithm

- More detail in Watt's 10.3.1 (pp.284-286) and 12.2-12.4 (pp.342-354)



Creating a Ray

- Parameters:
 - Image Plane (position, size, and resolution)
 - Viewpoint
 - Which ray (x, y)?



Ray-Object Intersection

- For example: sphere

$$(x-x_0)^2+(y-y_0)^2+(z-z_0)^2=r^2$$

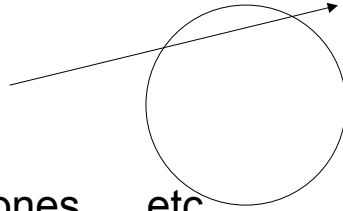
- Ray: $(x,y)=(x_1,y_1)+t(x_d,y_d)$

- Find t that satisfy

$$(x-x_0)^2+(y-y_0)^2+(z-z_0)^2=r^2$$

- Normal vector?

- Also easy for planes, cones, ...etc.

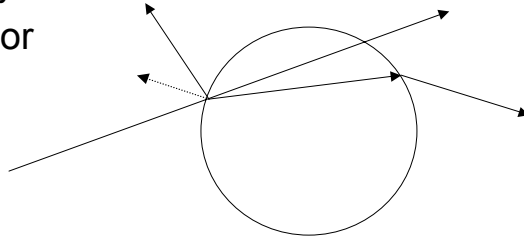


Shading Models

- Pixel color = ambient + diffuse + specular + reflected + transmitted
- The weight of each is determined by the surface properties.

Reflection and Refraction

- Reflected ray is determined by:
 - incoming ray and normal vector.
- Refracted ray is determined by:
 - Incoming ray
 - Normal vector
 - And density



Recursive Algorithm

- The reflected ray and refracted ray are traced recursively.
- Termination condition:
 - Depth of trace
 - Weight (to the final pixel color) of ray
- Pseudo code in Watt's page 349.

Advantage

- We get all the following automatically:
 - Hidden surface removal
 - Shadow
 - Reflection
 - Transparency and refraction

Disadvantage

- Slow. Many rays are spawned.
- Slow. Ray-object intersection for every ray and every object. (Space partition helps a lot!).
- The lighting is still not completely right!

Can you get
this with ray
tracing?



Other Global Illumination Techniques

- Radiosity
- Monte Carlo path tracing, for examples:
 - Distributed ray tracing
 - Metropolis light transport
 - Photon map...etc.
- Want to know more? Take Digital Image Synthesis next semester!

What is Radiosity

- Borrowed from radiative heat transfer.
- Assuming diffuse reflectance.
- View independent solution.



RADIANCE



© 1994 by Charles Ehrlich, Mark Mack

Photon Map



Metropolis Light Transport

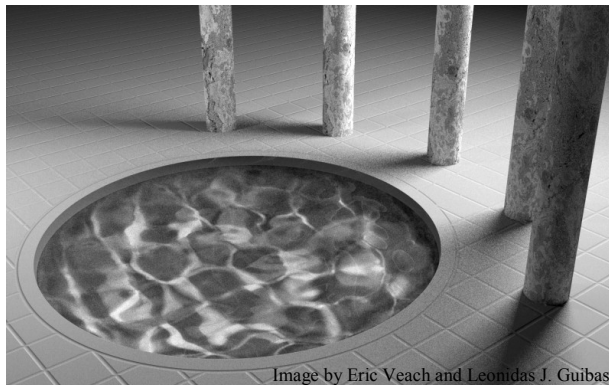


Image by Eric Veach and Leonidas J. Guibas